

Application of Integration

Choose the correct answer:-

5 x 1 = 5

1. The value of $\int_{-1}^2 |x| dx$ is

- (a) $\frac{1}{2}$ (b) $\frac{3}{2}$ (c) $\frac{5}{2}$ (d) $\frac{7}{2}$

2. If $f(x) = \int_0^x t \cos t dt$, then $\frac{df}{dx} = \dots\dots\dots$

- (a) $\cos x - \sin x$ (b) $\sin x + \cos x$ (c) $x \cos x$ (d) $x \sin x$

3. The value of $\int_0^1 (\sin^{-1}x)^2 dx$ is

- (a) $\frac{\pi^2}{4} - 1$ (b) $\frac{\pi^2}{4} + 2$ (c) $\frac{\pi^2}{4} + 1$ (d) $\frac{\pi^2}{4} - 2$

4. The area of the region bounded by the graph $y = \sin x$ and $y = \cos x$ between $x = 0$ and $x = \frac{\pi}{4}$ is

- (a) $\sqrt{2}$ (b) $\sqrt{2} - 1$ (c) $2\sqrt{2} - 2$ (d) $2\sqrt{2} + 2$

5. If $\frac{\gamma n + 2}{\gamma n} = 90$ then n is

- (a) 10 (b) 5 (c) 8 (d) 9

Answer any 5 of the following (Question no 8 is compulsory):-

5 x 2 = 10

6) $\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} (x^5 + x \cos x + \tan^3 x + 1) dx$

7) $\int_3^4 \frac{1}{x^2 - 4} dx$

8) Find, by integration, the volume of the solid generated by revolving about the x-axis, the region enclosed by $y=2x^2$, $y = 0$ and $x = 1$.

9) Find the volume of solid right circular cone with base radius 'r' and height 'h'.

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10) Find an approximate value of $\int_1^{1.5} x dx$ by applying the left-end rule with the partition $\{1.1, 1.2, 1.3, 1.4, 1.5\}$.

11) Prove that $\int_a^b f(x) dx = - \int_b^a f(x) dx$.

12) Find $\int_{-5}^5 x \cos x dx$.

13) Evaluate $\int_0^1 x(1-x)^n dx = \frac{1}{(n+1)(n+2)}$.

Answer any 5 of the following (Question no 21 is compulsory):-

7 x 3 = 21

14) Evaluate $\int_{\frac{\pi}{8}}^{\frac{3\pi}{8}} \frac{1}{1 + \sqrt{\cot x}} dx$

15) Evaluate $\int_b^{\infty} \frac{1}{x^2 + a^2} dx$, $a > 0$, b is a real number and hence deduce the value of

$\int_0^{\infty} \frac{1}{x^2 + a^2} dx$.

16) Evaluate $\int_0^{2\pi} \sin^7 \frac{x}{4} dx$.

17) Evaluate $\int_0^{\frac{\pi}{2}} \sin^5 x \cos^4 x dx$.

18) Evaluate $\int_0^1 |5x - 3| dx$

19) Evaluate $\int_0^{\infty} x^5 e^{-3x} dx$.

20) Find the area of the region bounded by $y = \tan x$ and $y = \cot x$ and the lines $x = 0$, $x = \frac{\pi}{2}$, $y = 0$.

21) Prove that $\int_0^{\frac{\pi}{4}} \log(1 + \tan x) = \frac{\pi}{8} \log 2$.

Answer the following:-

3 x 5 = 15

22) Find the area region common to the circle $x^2 + y^2 = 16$ and the parabola $y^2 = 6x$

[OR]

The slope of the curve $y = (x-2)^2 + 1$ has a minimum point at P. The point Q on the curve is such that the slope of PQ is 2. Find the area bounded by the curve and the chord PQ.

23) Evaluate $\int_0^{\frac{\pi}{2}} \frac{1}{1 + 5\cos^2 x} dx$.

[OR]

Evaluate $\int_2^3 \frac{\sqrt{x}}{\sqrt{5-x} + \sqrt{x}} dx$.

24) Using integration prove that the area of the triangle whose vertices are given by (0,0) , (5,0) and (2,3) is 7.5 sq units.

[OR]

Evaluate the following integrals as the limits of sums $\int_0^1 (5x + 4) dx$.

All the best